# DT2112 Speech Recognition by Computers

Giampiero Salvi

KTH/CSC/TMH giampi@kth.se

VT 2014

1 / 113

Notes

#### Motivation

- Natural way of communication (No training needed)
- ► Leaves hands and eyes free (Good for functionally disabled)
- ▶ Effective (Higher data rate than typing)
- Can be transmitted/received inexpensively (phones)

2 / 113

#### A dream of Artificial Intelligence



2001: A space odyssey (1968)

3/113

#### The ASR Scope

Convert speech into text



Not considered here:

- non-verbal signals
- prosody
- multi-modal interaction

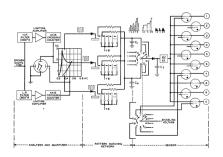
-			

# Notes

Notes

#### A very long endeavour

1952, Bell laboratories, isolated digit recognition, single speaker, hardware based [2]



[2] K. H. Davis, R. Biddulph, and S. Balashek. "Automatic Recognition of Spoken Digits". In: JASA 24.6 (1952), pp. 637–642

pp. 637–642

Notes			

#### An underestimated challenge

for 60 years many bold announcements

6 / 113

#### Applications today

#### Call centers:

- traffic information
- ▶ time-tables
- booking...

#### Accessibility

- Dictation
- ▶ hand-free control (TV, video, telephone)

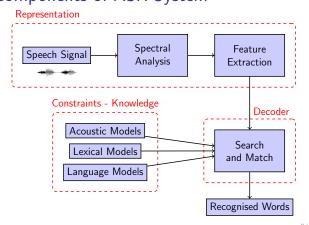
#### Smart phones

► Siri, Android...

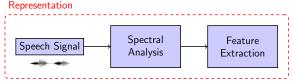
#### Notes

Notes

#### Components of ASR System



#### Speech Signal Representations



#### Goals:

- disregard irrelevant information
- optimise relevant information for modelling

#### Means

- try to model essential aspects of speech production
- imitate auditory processes
- consider properties of statistical modelling

11 / 113

Notes

#### **Examples of Speech Sounds**

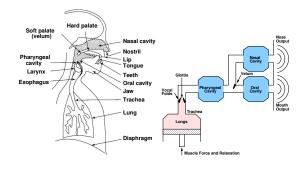


http://www.speech.kth.se/wavesurfer/

12 / 113

Notes				

#### Feature Extraction and Speech Production

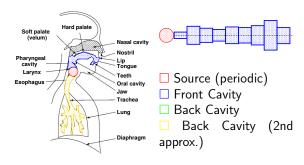


13 / 113

Notes			
-			

#### Source/Filter Model, General Case

#### Vowels

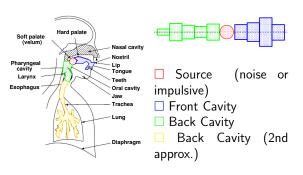


N	otes	
Ν	otes	

14000			

#### Source/Filter Model, General Case

Fricatives (e.g. sh) or Plosive (e.g. k)

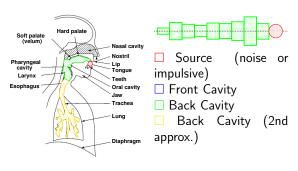


Notes

14 / 113

#### Source/Filter Model, General Case

Fricatives (e.g. s) or Plosive (e.g. t)



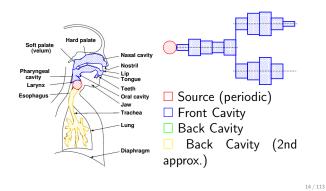
14 / 113

#### Notes

_				

#### Source/Filter Model, General Case

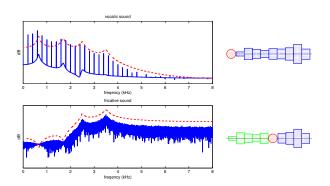
#### Nasalised Vowels



Notes

_			
_			
-			
-			

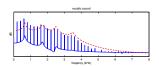
Examples



#### Relevant vs Irrelevant Information

For the purpose of transcribing words:

Relevant: vocal tract shape  $\rightarrow$  spectral envelope Irrelevant: vocal fold vibration frequency (f0)  $\rightarrow$ spectral details



#### Exceptions:

- tonal languages (Chinese)
- pitch and prosody convey meaning

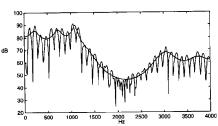
16 / 113

Notes

#### Linear Prediction Analysis

Attempt to model the vocal tract filter

$$\tilde{x}[n] = \sum_{k=1}^{p} a_k x[n-k]$$



better match at spectral peaks than valleys

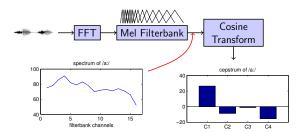
17 / 113

#### Mel Frequency Cepstrum Coefficients

- ▶ imitate aspects of auditory processing
- de facto standard in ASR
- does not assume all-pole model of the spectrum
- uncorrelated: easier to model statistically

18 / 113

#### MFCCs Calculation



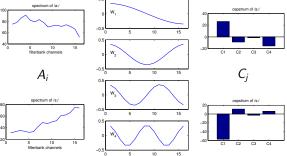
•		

Notes

Notes

Cosine Transform

$$C_j = \sqrt{\frac{2}{N}} \sum_{i=1}^{N} A_i \cos(\frac{j\pi(i-0.5)}{N})$$



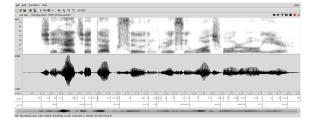
Notes

MFCCs: typical values

- ▶ 12 Coefficients C1–C12
- ► Energy (could be C0)
- ▶ Delta coefficients (derivatives in time)
- ▶ Delta-delta (second order derivatives)
- ► total: 39 coefficients per frame (analysis window)

21 / 113

A time varying signal



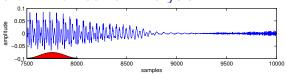
- speech is time varying
- short segment are quasi-stationary
- use short time analysis

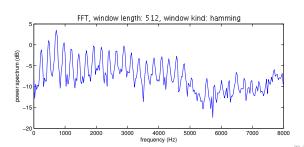
22 / 113

Notes

Notes

Short-Time Fourier Analysis



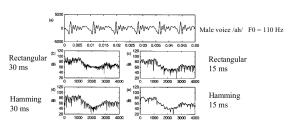


# Short-Time Fourier Analysis Output O



#### Short-Time Fourier Analysis

Effect of different window functions



Window should be long enough to cover 2 pitch pulses Short enough to capture short events and transitions

23 / 113

#### Windowing, typical values

▶ signal sampling frequency: 8–20kHz

▶ analysis window: 10–50ms

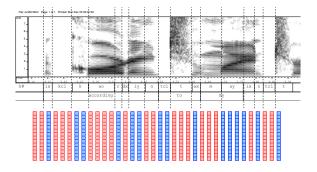
• frame interval: 10–25ms (100–40Hz)

Notes

Notes

24 / 113

#### Frame-Based Processing



#### Comparing frames

• city block distance:  $d(x, y) = \sum_{i} |x_i - y_i|$ 

▶ Euclidean distance:  $d(x,y) = \sqrt{\sum_i (x_i - y_i)^2}$ 

Mahalanobis distance:  $d(x, y) = \sum_{i} (x_i - \mu_y)^2 / \sigma_y$ 

▶ probability function:

 $f(X = x | \mu, \Sigma) = N(x; \mu, \Sigma)$ 

• artificial neural networks:  $d = f(\sum_i w_i x_i - \theta)$ 

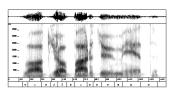
26 / 113

Notes

#### **Comparing Utterances**

In order to recognise speech we have to be able to compare different utterances



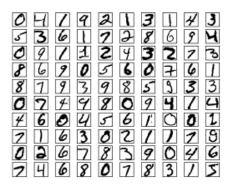


Va jobbaru me

Vad jobbar du med

27 / 113

#### Fixed vs Variable Length Representation



28 / 113

# Combining frame-wise scores into utterance scores

Template Matching

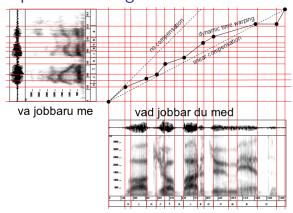
- oldest technique
- simple comparison of template patterns
- compensate for varying speech rate (Dynamic Programming)

Hidden Markov Models (HMMs)

- most used technique
- models of segmental structure of speech
- recognition by Viterbi search (Dynamic Programming)

Notes				
Notes				
	Notes			
	Notes			
Notes	Notes			
Notes				
	Votes			

#### Template Matching

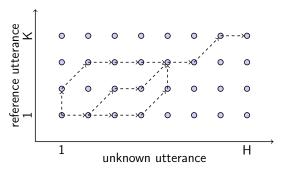


Notes

31 / 113

#### Dynamic Programming

- ▶ compare any possible alignment
- problem: exponential with H and K!



32 / 113

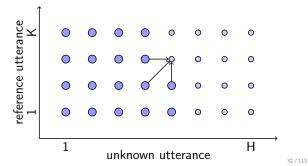
Notes

Dynamic Programming

Dynamic Time Warping (DTW) algorithm

1: **for** h = 1 to H **do**2: **for** k = 1 to K **do** 

 $\begin{array}{ll} \text{AccD[}h,k] = LocD[}h,k] + \min(AccD[}h-1,k],AccD[}h-1,k-1],AccD[}h,k-1]) \end{array}$ 



Notes

#### DP Example: Spelling

- observations are letters
- ▶ local distance: 0 (same letter), 1 (different letter)
- Unknown utterance: ALLDRIG

Reference1: ALDRIGReference2: ALLTID

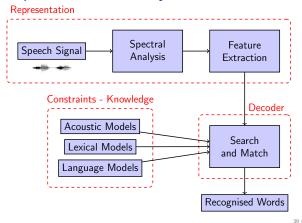
Problem: find closest match

Distance char-by-char:

- ► ALLDRIG-ALDRIG = 5
- ► ALLDRIG-ALLTID = 4

DP Example: Solution	Notes
LocD[h,k] = AccD[h,k] =	
G 1 1 1 1 1 1 0 G 5 4 4 3 2 1 0 I 1 1 1 1 1 0 1 I 4 3 3 2 1 0 1 R 1 1 1 1 0 1 1 R 3 2 2 1 0 1 2 D 1 1 1 0 1 1 1 D 2 1 1 0 1 2 3 L 1 0 0 1 1 1 1 L 1 0 0 1 2 3 4 A 0 1 1 1 1 1 1 A 0 1 2 3 4 5 6	
A L L D R I G A L L D R I G	
Distance ALLDRIG-ALDRIG: $AccD[H,K] = 0$	
Distance ALLDRIG-ALLTID?  34/113	
DP Example: Solution $LocD[h,k] = AccD[h,k] =$	Notes
D 1110111 D 5332333	
I 1 1 1 1 1 0 1 I 4 2 2 2 2 2 3 T 1 1 1 1 1 1 1 T 3 1 1 1 2 3 4	
L 1001111 L 2001234 L 1001111 L 1001234	
A 0 1 1 1 1 1 1 A 0 1 2 3 4 5 6	
A L L D R I G A L L D R I G	
Distance ALLDRIG-ALDRIG: $AccD[H,K] = 0$ Distance ALLDRIG-ALLTID: $AccD[H,K] = 3$	
### DISTAILER ALLETTO. ACCD[11,N] = 3  ### 35/113	
Best path: Backtracking	Notes
Sometimes we want to know the path  1. at each point [h,k] remember the minimum	
distance predecessor (back pointer)	
<ol><li>at the end point [H,K] follow the back pointers until the start</li></ol>	
36/113	
Properties of Template Matching	Notes
+ No need for phonetic transcriptions	
<ul><li>+ within-word co-articulation for free</li><li>+ high time resolution</li></ul>	
Cons:  — cross-word co-articulation not modelled	
<ul> <li>requires recordings of every word</li> </ul>	
<ul><li>not easy to model variation</li><li>does not scale up with vocabulary size</li></ul>	

#### Components of ASR System



Notes

#### A probabilistic perspective

- 1. Compute probability of a word sequence given the acoustic observation: *P*(words|sounds)
- 2. find the optimal word sequence by maximising the probability:

 $\widehat{\mathsf{words}} = \mathsf{arg}\,\mathsf{max}\,P(\mathsf{words}|\mathsf{sounds})$ 

40 / 113

#### A probabilistic perspective: Bayes' rule

$$P(\mathsf{words}|\mathsf{sounds}) = \frac{P(\mathsf{sounds}|\mathsf{words})P(\mathsf{words})}{P(\mathsf{sounds})}$$

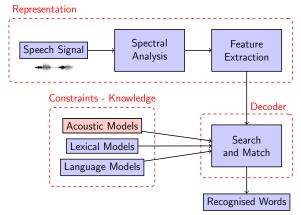
- ► P(sounds|words) can be estimated from training data and transcriptions
- ► P(words): a priori probability of the words (Language Model)
- ► P(sounds): a priori probability of the sounds (constant, can be ignored)

41 / 113

Notes

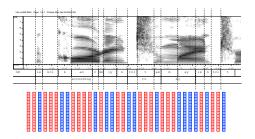
Notes

#### Components of ASR System



#### Probabilistic Modelling

Problem: How do we model P(sounds|words)?



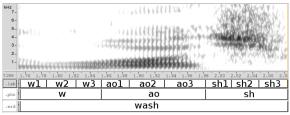
Every feature vector (observation at time t) is a continuous stochastic variable (e.g. MFCC)

43 / 113

#### Stationarity

Problem: speech is not stationary

- ▶ we need to model short segments independently
- ► the fundamental unit can not be the word, but must be shorter
- usually we model three segments for each phoneme



Notes

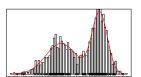
Notes

#### Local probabilities (frame-wise)

If segment sufficiently short

P(sounds|segment)

can be modelled with standard probability distributions Usually Gaussian or Gaussian Mixture

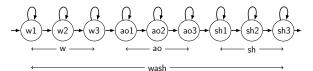


# Notes

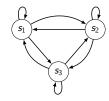
#### Global Probabilities (utterance)

Problem: How do we combine the different P(sounds|segment) to form P(sounds|words)?

Answer: Hidden Markov Model (HMM)




#### Hidden Markov Models (HMMs)



#### Elements:

set of states: transition probabilities: prior probabilities: state to observation probabilities:

$$S = \{s_1, s_2, s_3\}$$

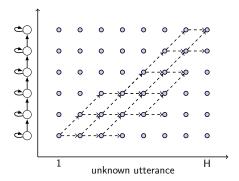
$$T(s_a, s_b) = P(s_b, t | s_a, t - 1)$$

$$\pi(s_a) = P(s_a, t_0)$$

$$B(o, s_a) = P(o | s_a)$$

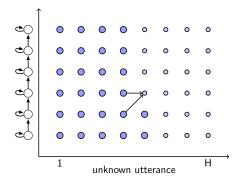
# Notes

#### Hidden Markov Models (HMMs)



Notes

#### Hidden Markov Models (HMMs)



Notes

_			
_			
_			
_			

**HMM**-questions

- 1. what is the probability that the model has generated the sequence of observations? (isolated word recognition) forward algorithm
- 2. what is the most likely state sequence given the observation sequence? (continuous speech recognition) Viterbi algorithm [5]
- 3. how can the model parameters be estimated from examples? (training) Baum-Welch[1]

<sup>[5]</sup> A. J. Viterbi. "Error Bounds for Convolutional Codes and an Asymtotically optimum decoding algorithm". In IEEE Trans. Inform. Theory IT-13 (Apr. 1967), pp. 260–269

### Isolated Words Recognition Notes hmm1 hmm2 hmm3 hmmK Compare Likelihoods (forward-backward) 50 / 113 Continuous Speech Recognition Notes $\mathsf{hmm1}$ hmm2 hmm3 $\mathsf{hmmK}$ Viterbi algorithm 51 / 113 Modelling Coarticulation Notes Example peat /pi:t/ vs wheel /wi:l/ 2000 0.1 0.2 0.3 Time (seconds) 0.1 0.2 0. Time (seconds) 52 / 113 Modelling Coarticulation Notes Context dependent models (CD-HMMs) ▶ Duplicate each phoneme model depending on left and right context: ▶ from "a" monophone model ▶ to "d-a+f", "d-a+g", "l-a+s"... triphone

If there are N = 50 phonemes in the language, there are N³ = 125000 potential triphones
 ▶ many of them are not exploited by the language

53 / 11

#### Amount of parameters

Example:

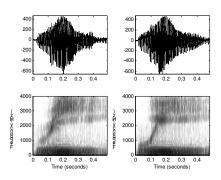
- ► a large vocabulary recogniser may have 60000 triphone models
- each model has 3 states
- each state may have 32 mixture components with  $1 + 39 \times 2$  parameters each (weight, means, variances):  $39 \times 32 \times 2 + 32 = 2528$

Totally it is  $60000 \times 3 \times 2528 = 455$  million parameters!

54 / 113

#### Similar Coarticulation

/riː/ vs /wiː/



55 / 113

#### Tying to reduce complexity

Example: similar triphones d-a+m and t-a+m

- same right context, similar left context
- ▶ 3rd state is expected to be very similar
- 2nd state may also be similar

States (and their parameters) can be shared between models

- + reduce complexity
- + more data to estimate each parameter
- fine detail may be lost

done with CART tree methodology

56 / 113

#### Components of ASR System

Speech Signal Spectral Analysis Feature Extraction

Constraints - Knowledge Decoder

Acoustic Models Search and Match

Language Models

Recognised Words

Notes

Notes

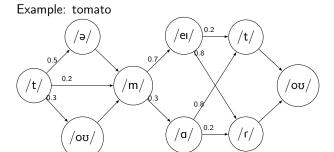
#### Lexical Models

- ▶ in general specify sequence of phoneme for each word
- example:

- expensive resources
- include multiple pronunciations
- phonological rules (assimilation, deletion)

58 / 113

#### Pronunciation Network



59 / 11

#### Assimilation

did you /d ι dʒ j ə/
set you /s ε tʃ з/
last year /l æ s tʃ iː ɹ/
because you've /b iː k ə ʒ uː v/

60 / 113

#### Deletion

find him /f aιnιm/ around this /ə ι aʊ n ι s/ let me in /l ε m iː n/

Notes

Notes

Notes

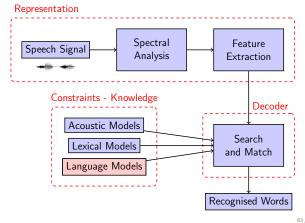
 ${\sf Notes}$ 

#### Out of Vocabulary Words

- ▶ Proper names often not in lexicon
- derive pronunciation automatically
- ► English has very complex grapheme-to-phoneme rules
- attempts to derive pronunciation from speech recordings

62 / 113

#### Components of ASR System



Notes

Notes

#### Why do we need language models?

Bayes' rule:

$$P(words|sounds) = \frac{P(sounds|words)P(words)}{P(sounds)}$$

where

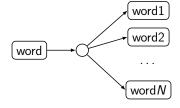
P(words): a priori probability of the words (Language Model)

We could use non informative priors (P(words) = 1/N), but...

Notes

#### **Branching Factor**

- ▶ if we have N words in the dictionary
- ► at every word boundary we have to consider *N* equally likely alternatives
- N can be in the order of millions



N	ot	es
	υı	<u></u>

64 / 113

Ambiguity	Notes
"ice cream" vs "I scream" /агs k л iː m/	
66/113	
Language Models	Notes
$P(words sounds) = \frac{P(sounds words)P(words)}{P(sounds)}$ Finite state networks (hand-made, see lab) • formal language, e.g. traffic control Statistical Models (N-grams) • unigrams: $P(w_i)$ • bigrams: $P(w_i w_{i-1})$ • trigrams: $P(w_i w_{i-1},w_{i-2})$ •	
Chomsky's formal grammar	Notes
Noam Chomsky: linguist, philosopher, $G = (V, T, P, S)$	
<pre>where  V: set of non-terminal constituents T: set of terminals (lexical items) P: set of production rules S: start symbol</pre>	
Example $S = \text{ sentence } V = \{ \text{NP (noun phrase), } \\ \text{NP1, VP (verb phrase), NAME, ADJ, } V (\text{verb), N (noun)} \}$ $T = \{ \text{Mary , person , loves } \\ \text{, that ,} \}$ $P = \{ \text{S} \rightarrow \text{NP VP } \\ \text{NP} \rightarrow \text{NAME } \\ \text{NP} \rightarrow \text{ADJ NP1 } \\ \text{NP1} \rightarrow \text{N} \\ \text{VP} \rightarrow \text{VERB NP } \\ \text{NAME} \rightarrow \text{Mary} $ that	Notes

 $V \rightarrow loves$   $N \rightarrow person$  $ADJ \rightarrow that$  }

### Formal Language Models Notes only used for simple tasks hard to code by hand people do not speak following formal grammars 70 / 113 Statistical Grammar Models (N-grams) Notes Simply count co-occurrence of words in large text data sets • unigrams: $P(w_i)$ ▶ bigrams: $P(w_i|w_{i-1})$ • trigrams: $P(w_i|w_{i-1},w_{i-2})$ 71 / 113 Language Models: complexity Notes Increasing N in N-grams leads to: 1. more complex decoders 2. difficulties in training the LM parameters 72 / 113 Knowledge Models in ASR Notes Acoustic Models trained on hours of annotated speech recordings (especially developed speech databases) Lexical Model usually produced by hand by experts (or generated by rules) Language Models trained on millions of words of

text (often from news papers)

#### Main variables in ASR

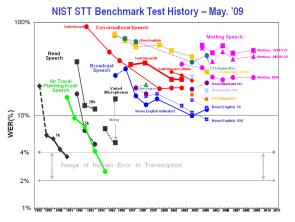
Speaking mode isolated words vs continuous speech
Speaking style read speech vs spontaneous speech
Speakers speaker dependent vs speaker
independent

Vocabulary small (<20 words) vs large (>50 000 words)

Robustness against background noise

75 / 113

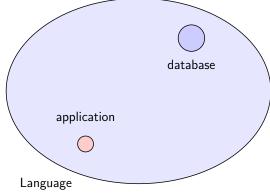
Notes



http://www.itl.nist.gov/iad/mig/publications/ASRhistory/

76 / 11

#### Why is it so hard?



77 / 113

#### Challenges — Variability

#### Between speakers

- Age
- Gender
- Anatomy
- Dialect

#### Within speaker

- Stress
- Emotion
- ► Health condition
- ▶ Read vs Spontaneous
- Adaptation to environment (Lombard effect)
- Adaptation to listener

#### Environment

- Noise
- Room acoustics
- Microphone distance
- ▶ Microphone, telephone
- ► Bandwidth

#### Listener

- Age
- ► Mother tongue
- Hearing loss
- ► Known / unknown
- ▶ Human / Machine

Votes			
Notes			
10100			
Notes			

#### Sheep and Goats [3]



[3] G. Doddington, W. Liggett, A. Martin, M. Przybocki, and D. Reynolds. "SHEEP, GOATS, LAMBS and WOLVES A Statistical Analysis of Speaker Performance in the NIST 1998 Speaker Recognition Evaluation". In:

70 / 113

#### A Statistical Analysis of Speaker Fertomatice in the 1931 1996 Speaker Recognition Evaluation ... INTERNATIONAL CONFERENCE ON SPOKEN LANGUAGE PROCESSING. 1998

#### Sheep and Goats [3]



[3] G. Doddington, W. Liggett, A. Martin, M. Przybocki, and D. Reynolds. "SHEEP, GOATS, LAMBS and WOLVES A Statistical Analysis of Speaker Performance in the NIST 1998 Speaker Recognition Evaluation". In: INTERNATIONAL CONFERENCE ON SPOKEN LANGUAGE PROCESSING. 1998

79 / 113

#### Exmpl: spontaneous vs hyper-articulated



Va jobbaru me

Vad jobbar du med

"What is your occupation" ("What work you with")

80 / 113

#### Examples of reduced pronunciation

Spoken	Written	In English
Tesempel	Till exempel	for example
åhamba	och han bara	and he just
bafatt	bara för att	just because
javende	jag vet inte	I don't know

Notes

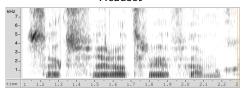
Notes

#### Notes

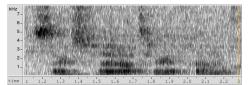
-

#### Microphone distance

#### Headset



2 m distance



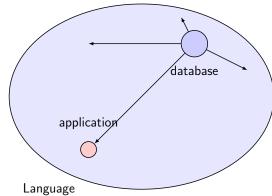
#### Notes

-			

82 / 113

#### How do we cope with variability?

Ideally: models that generalise



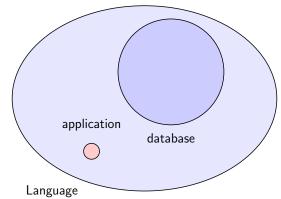
83 / 113

84 / 113

#### Notes

How do we cope with variability?

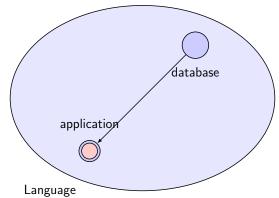
Large companies use insane quantities of data



Notes


How do we cope with variability?

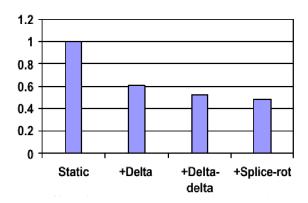
Adaptation



Notes

#### Adaptation: Example Notes Enrolment in Dictation Systems ▶ let the user read a small text before using the system Beta version of smartphone applications the company has all the rights on data generated Word Accuracy Notes $A=100\frac{N-S-D-I}{N}$ Where N: total number of reference words ▶ *S*: substitutions D: deletions I: insertions 88 / 113 Word Accuracy: example Notes Ref/Rec | - [ wanted | badly | meet | you to corr really del wanted corr to ins corr sub see you corr 6 words, 1 substitution, 1 insertion, 1 deletion $A = 100 \frac{6 - 1 - 1 - 1}{6} = 50\%$ requires dynamic programming Measure Difficulty Notes Language Perplexity $B = 2^H$ , $H = -\sum_{\forall W} P(W) \log_2(P(W))$ $\triangleright P(W)$ is the probability of the word sequence (language model) H is called entropy ▶ B can be seen as measure of average number of words that can follow any given word • Example: equiprobable digit sequences B = 10

#### Effect of adding features

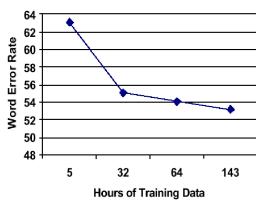


Notes

91 / 113

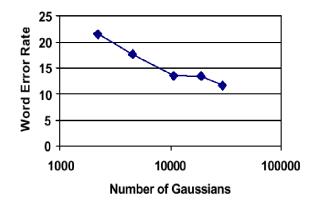
#### Effect of adding training data

Swichboard data



Notes

Effect of adding Gaussians



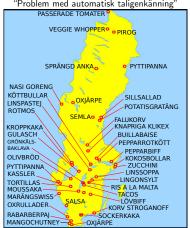
Notes

93 / 113

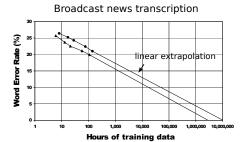
#### Effect of adding data for language models

55 50 45 40 35 30 1 10 100 1000 8300 Million sentences

# Some dictation systems Notes vocabulary over 100 000 words many languages systems: Nuance NatuallySpeaking, Microsoft, (IBM ViaVoice), (Dragon Dictate) 95 / 113 New applications Notes ▶ Indexing of TV and radio programs (offline), Google real-time subtitling of TV programs (re-speaker that summarises) language learning smart phones Limitations Notes ▶ lack of context require huge amounts of training data Adapted from Mikael Parkvall's Lingvistiska Samlarbilder, Nr.96: "Problem med automatisk taligenkänning" PASSERADE TOMATER O Notes VEGGIE WHOPPER® PIROG



#### Lack of Generalisation[4]



In order to reach 10-years-old's performance, ASR needs 4 to 70 human lifetimes exposure to speech!!

[4] R. Moore. "A Comparison of the Data Requirements of Automatic Speech Recognition Systems and Human 99 / 113 Listeners" In: Proc. of Furginger Geneva, Switzerland, 2003, pp. 2582–2584.

## New directions

- ▶ Production inspired modelling
- Study children's speech acquisition
- Modelling and decision techniques
  - Eigenvoices
  - ► Deep learning neural networks

100 / 113

#### Speaker Recognition



Created by Håkan Melin

102 / 113

#### Person Identification

Methods rely on:

- something you posses: key, magnetic card, ...
- ► something you know: PIN-code, password, . . .
- something you are: physical attributes, behaviour (biometrics)

Notes			
N.I			
Notes			
Notes			
Notes			

#### Recognition, Verification, Identification

Recognition: general term Speaker verification:

- ▶ an identity is claimed and is verified by voice
- binary decision (accept/reject)
- performance independent of number of users

#### Speaker identification:

- choose one of N speakers
- close set: voice belongs to one of the N speakers
- open set: any person can access the system
- problem difficulty increases with N

104 / 113

Notes

#### Text Dependence

Either fix the content or recognise it. Examples:

- Fixed password (text dependent)
- User-specific password
- System prompts the text (prevents impostors from recording and playing back the password)
- any word is allowed (text independent)

text independent

105 / 113

Notes

#### Representations

Speech Recognition:

- represent speech content
- disregard speaker identity

Speaker Recognition:

- ▶ represent speaker identity
- disregard speech content

Surprisingly:

- MFCCs used for both
- suggests that feature extraction could be improved

106 / 113

#### Speaker Verification

Registration (train	ning, enrolment)	
	Trained speaker me	odel
Training utterances from a new client	Spectral analysis model	
Verification  Access utterance	Spectral analysis Matching Accept / Reject	•
	Claimed identity  Problem: The matching scor between the client model an utterance is sensitive to distortion, utterance duration	d the

NI - +				
Notes				

Notes		
Notes		

#### Modelling Techniques

**HMMs** 

- ► Text dependent systems
- ▶ state sequence represents allowed utterance

GMMs (Gaussian Mixture Models)

- ► Text independent systems
- ▶ large number of Gaussian components
- sequential information not used

SVM (Support Vector Machines)

Combined models

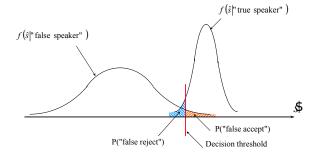
108 / 113

#### **Evaluation**

Claimed	Decision:			
Identity	Accept	Reject		
True	OK	False Reject (FR)		
False	False Accept (FA)	OK		

109 / 113

#### Score Distribution and Error Balance



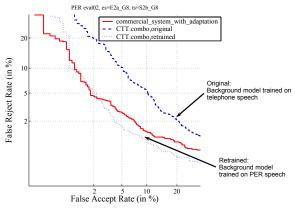
110 / 113

#### Performance Measures

- ► False Rejection Rate (FR)
- ▶ False Acceptance Rate (FA)
- ▶ Half Total Error Rate (HTER = (FR+FA)/2)
- ► Equal Error Rate (EER)
- ▶ Detection Error Trade-off (DET) Curve

Notes			
Notes			
Notes			

# PER vs Commercial System PER eval02, es=E2a\_G8, ts=S2b\_G8



112 / 113

More	information	and	mathematica
	formulations	s in	DT2118

113 / 113

Notes	
Notes	
Notes	
Notes	
Notes	