

# Information Theoretic Security

## Fall semester, 2013

Assignment 2

Assigned: Thursday, September 26, 2013

Due: Wednesday, October 9, 2013

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### ***Problems***

#### **Problem 1.1:**

Suppose that in a public key framework, Alice and Bob have key pairs  $(K_{pu}^A, K_{pr}^A)$  and  $(K_{pu}^B, K_{pr}^B)$ , respectively (subscript  $pu$  is referred to public key and the subscript  $pr$  is referred to private key). Alice intends to send message  $m$  to Bob. Give a scheme to sign the message and simultaneously securing that (providing confidentiality of the message).

#### **Problem 1.2:**

One approach to share a secret key between two entities is DiffieHellman key exchange protocol instead of establishing a secure channel between them. Describe this protocol. How is “the Man in the Middle Attack” resolved in this protocol?

#### **Problem 1.3:**

Each of AH and ESP protocols of IPsec can work in two modes; TRANSPORT and TUNNEL. Describe these two modes of IPsec and their differences.

#### **Problem 1.4:**

Show that the perfect security is compromised if two different messages are encrypted with a same key in One-Time Pad algorithm (which is described in slide #7 of the second lecture).

#### **Problem 1.5:**

Show that to provide perfect secrecy in One-Time Pad algorithm, the redundancy should be completely removed from the keystream (suppose that in key stream  $K = (k_1, k_2, \dots, k_n)$  there is correlation between  $i$ -th and  $j$ -th bits as  $k_i = k_j \oplus e$  where  $e$  is a binary random variable such that  $\Pr\{e = 1\} = p$  where  $0 \leq p < \frac{1}{2}$ ) and show that the perfect security is compromised, i.e.,  $I(M; C) \neq 0$ .

#### **Problem 1.6:**

Describe the relation between the three properties of the hash functions (pre-image resistance,

weak collision resistance and strong collision resistance), which implies the other one?