# Department of Mathematics 

SF1626
Several Variable Calculus
Academic year 2016/2017, Period 2

## Seminar 1

See www.kth.se/social/course/SF1626 for information about how the seminars work and what you are expected to do before and during the seminars.

This seminar will start with a hand-in of one of the problems. Solve problems 1-4 below and write down your solutions on separate sheets. Write your name and personal number on the top of each page. When the seminar starts you will be informed about which problem to hand in. Before starting with the seminar problems you should solve the recommended exercises from the text book Calculus by Adams and Essex (8th edition). These exercises are:

| Section | Recommended problems |
| ---: | :--- |
| $10.1:$ | $11,25,27,29,31,33,35,37,39$ |
| $10.6:$ | $3,5,9,13$ |
| $11.1:$ | $17,21,33$ |
| $11.2:$ | 3 |
| $11.3:$ | $5,7,11,13,15$ |
| $12.1:$ | $5,9,13,15,17,23,27,33$ |
| $12.2:$ | $5,7,9,11,15$ |

## Problems

Problem 1. Consider the sets in the $x y$-plane given by

$$
\begin{aligned}
& D_{1}=\left\{(x, y): 0<y-x^{2}, y=x\right\} \\
& D_{2}=\left\{(x, y): 0 \leq y^{2}-x, x^{2}+y^{2}<1\right\} \\
& D_{3}=\{(x, y):|x| \leq 1,|y| \leq 2\}
\end{aligned}
$$

(a) Sketch the sets $D_{1}, D_{2}$ and $D_{3}$.
(b) Mark the inner points of the sets.
(c) Mark the boundary points of the sets.
(d) Determine which of the sets are open, closed, or neither open nor closed.

Problem 2. Consider the cylinder $S$ given by the equation $x^{2}+y^{2}=1$ and let $C$ be the curve that describes the intersection of the cylinder with the plane defined by the equation $a x+b y+c z=0$.

Find a parametrisation $\mathbf{r}(t)$ of the curve $C$ when
(a) $a=b=0, \quad c=1$,
(b) $b=c=1, \quad a=0$,
(c) $a=b=1, \quad c=0$,
(d) $a=b=c=1$.

Problem 3. A particle travels in an orbit that is described by

$$
\mathbf{r}(t)=(1-t, \cos 2 t,-\sin 2 t),
$$

(a) Compute the velocity $\mathbf{r}^{\prime}(t)$.
(b) Compute the acceleration $\mathbf{r}^{\prime \prime}(t)$.
(c) Show that the velocity and the acceleration are perpendicular.

Problem 4. Let $f(x, y)=10 x^{2}+6 x y+13 y^{2}$ for all $(x, y)$ in $\mathbb{R}^{2}$.
(a) Make the change of variables given by $u=3 x+2 y$ and $v=x-3 y$, and express the function in terms of the variables $u$ and $v$.
(b) Sketch some of the level curves of the function $f$.
(c) Sketch the graph of the function $f$.
(d) Find a parametrization of the curve that is given by the intersection of the graph of the function $f$ and the plane defined by the equation $z=x-y$.

