

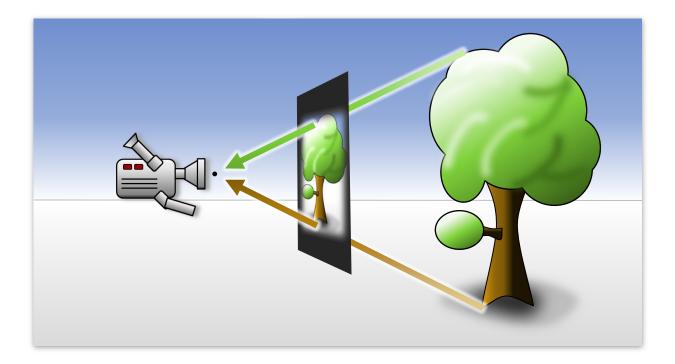
Introduction to Visualization and Computer Graphics DH2320, Fall 2015 Prof. Dr. Tino Weinkauf

#### Introduction to Visualization and Computer Graphics

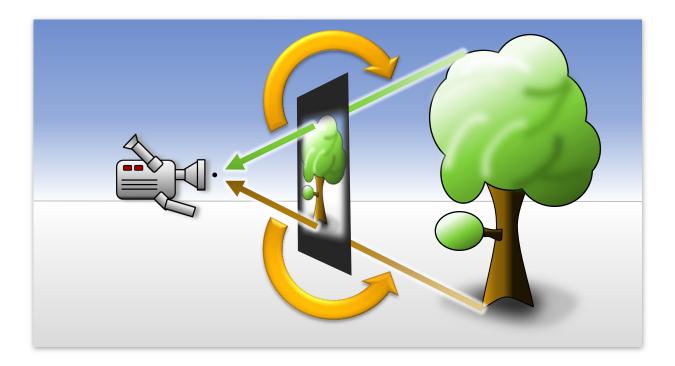
Raytracing

# **Basic Raytracing**

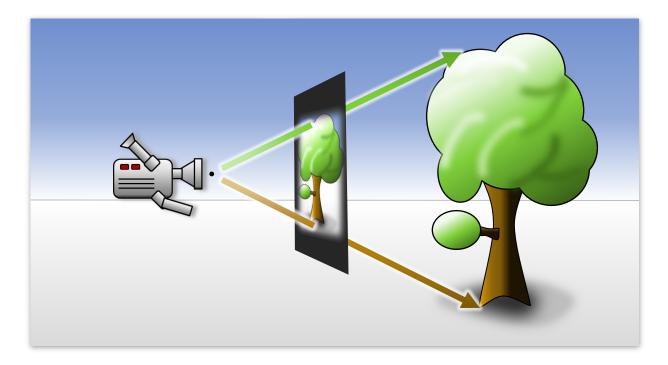
## **Central Projection**



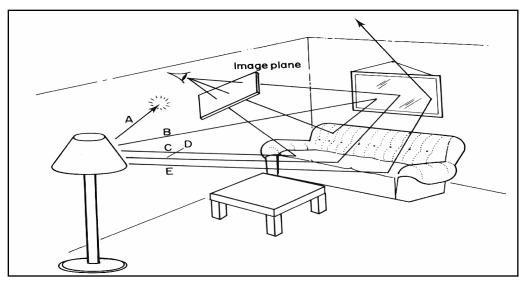
## **Central Projection**



## Ray Tracing

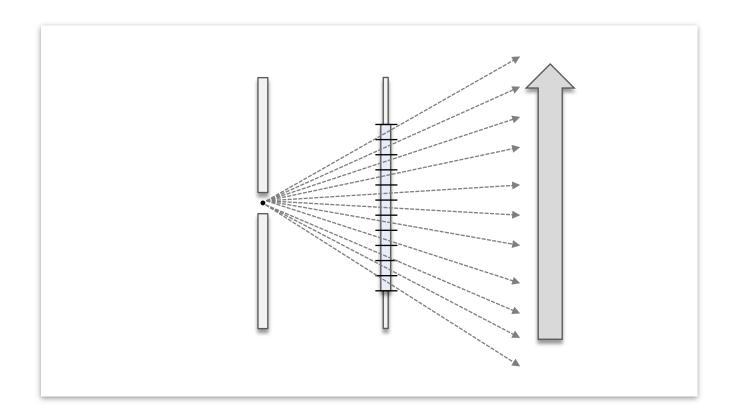


Some light rays (like A and E) never reach the image plane at all. Others follow simple (like C) or complicated routes. In general, it would be impractical to analyze all possible light paths because most of them do not have any practical influence on the generated image (do not intersect the image plane). In ray tracing, light rays are processed in inverse direction. It is assumed that all rays start at the eye of an observer (the viewing point), pass through the image plane toward objects in a scene, and finally reach the light sources. This approach reduces the number of traced light rays.



Introduction to Visualization and Computer Graphics, Tino Weinkauf, KTH Stockholm, Fall 2015

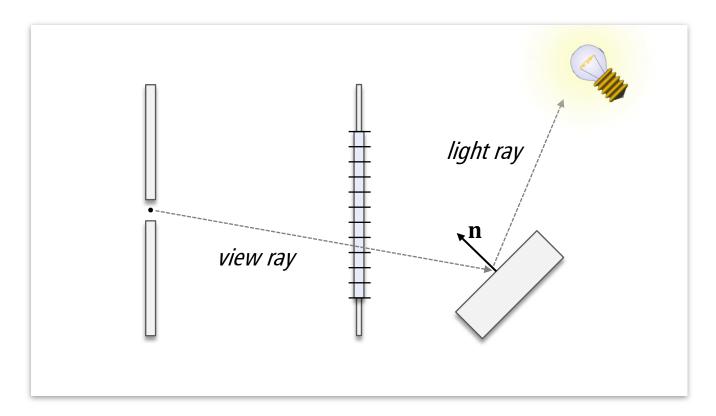
## **Ray Tracing**



#### **Primary Rays**

Rays through each pixel

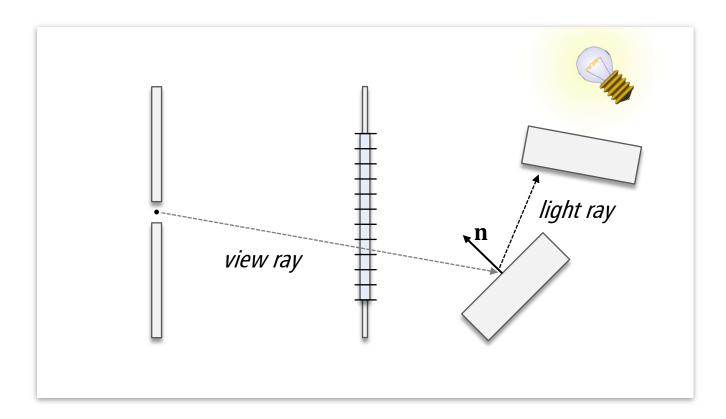
## Local Illumination



#### **Primary Rays**

- Rays through each pixel
- (Basic trigonometry)

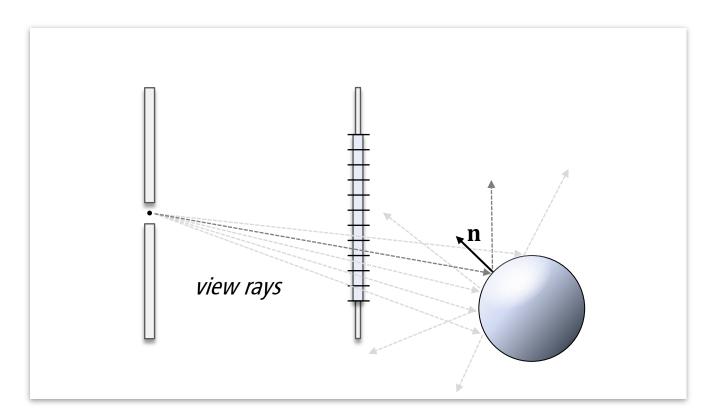
### Shadows



#### **Shadow rays**

Blocked by occluders (hard shadows)

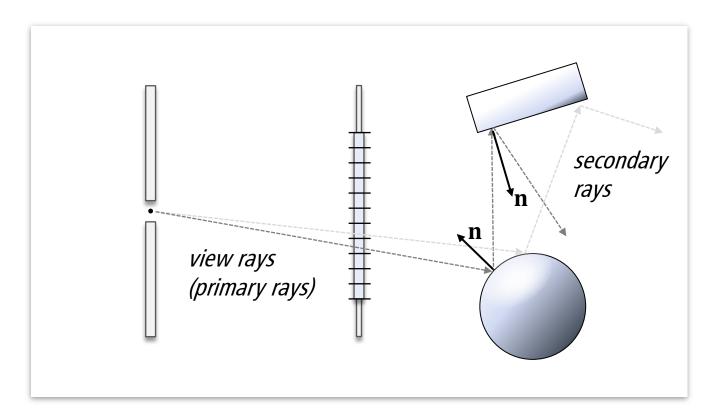
## Reflection



### Reflection

- Reflect ray across normal at intersection point
- (Basic linear algebra)

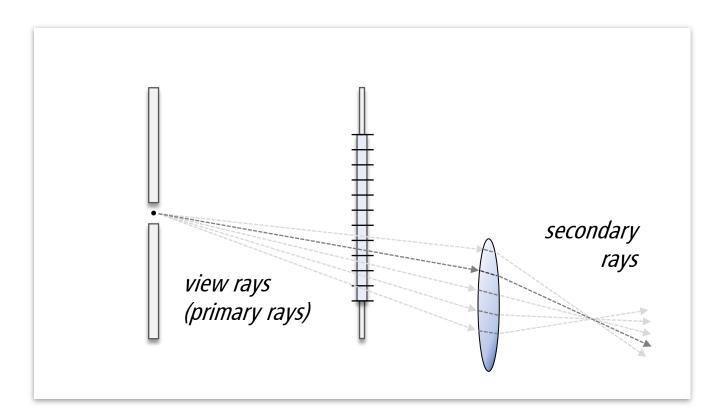
## Multiple Reflections: Recursion



#### **Multiple Reflections**

- Call algorithm recursively for secondary rays
- (Terminate after *n* levels, for safety)

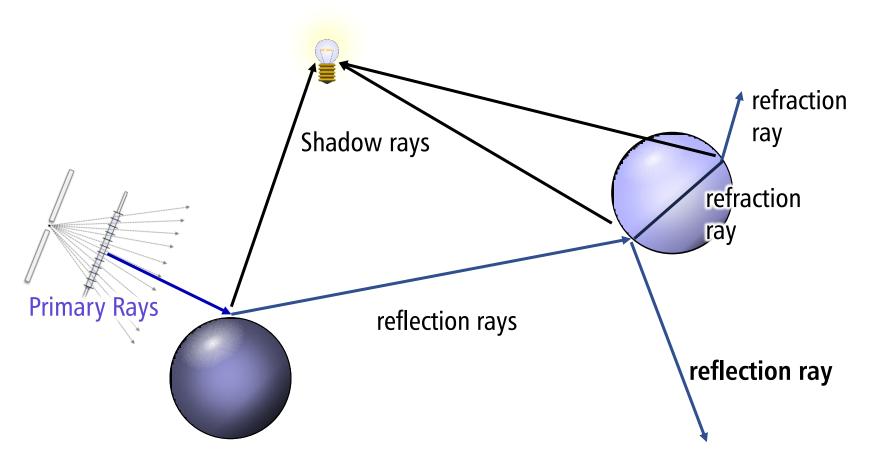
## Refraction



### Refraction

- Same story
- New rays: Snellius' law

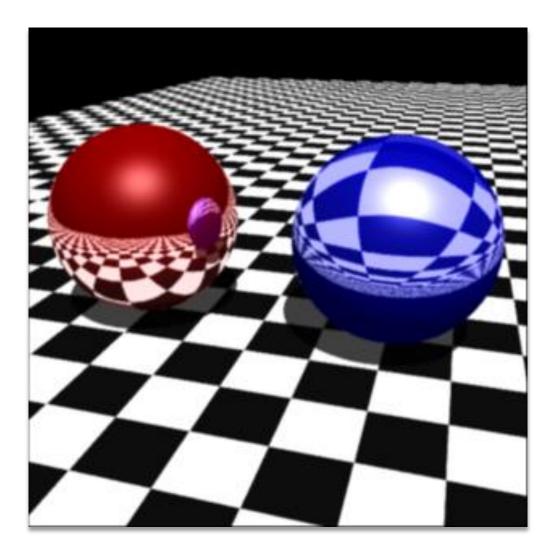
## **Recursive Raytracing**



#### Worst-case complexity

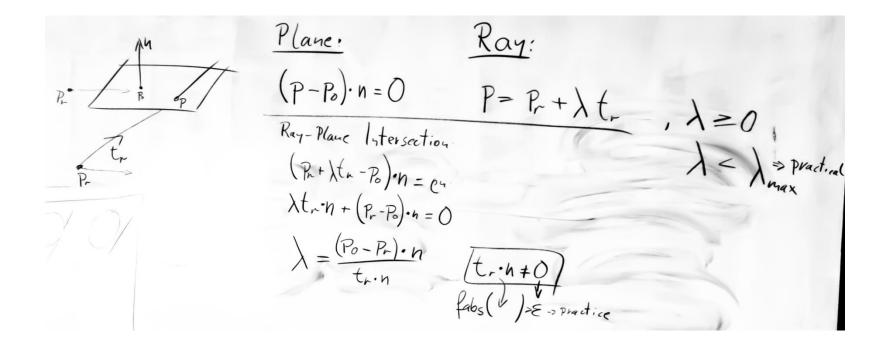
- $\mathcal{O}(\mathbf{n} \cdot \mathbf{m} \cdot 2^r)$
- *n* = Triangles, *m* = Pixels, *r* = maximum recursion depth

### Raytracing in a Nutshell



## **Intersection Tests**

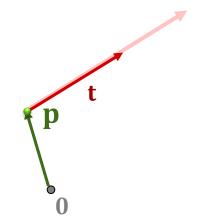
- Ray-Plane
- Ray-Triangle



Ray-Triangle A Intersection Possible Plane Equation.  $t_1 = P_1 - P_0$  $t_2 = P_2 - P_0$  $P = P_0 + \lambda_1 t_1 + \lambda_2 t_2$ λ, λ ∈ IR ⇒ Plane Po Pz  $h=t_1 \times t_2$  $\lambda_1, \lambda_2 \ge 0$ Andz=1 within triangle Pr Ray-Plane - Intersection V PETriangle?  $\lambda_1 + \lambda_2 \leq 1$ 

Introduction to Visualization and Computer Graphics, Tino Weinkauf, KTH Stockholm, Fall 2015

### **Ray-Sphere Intersection**



**Parametric line equation:** 

$$\mathbf{x}(\lambda) = \mathbf{p}_r + \lambda \mathbf{t}_r$$
$$\lambda \ge 0$$

$$r^2 y^2$$
  
 $r^2 y^2$   
 $x^2$ 

Sphere (Implicit!)

$$\langle \mathbf{x} - \mathbf{c}, \mathbf{x} - \mathbf{c} \rangle = r^2$$

$$\langle \mathbf{x}(\lambda) - \mathbf{c}, \mathbf{x}(\lambda) - \mathbf{c} \rangle - r^2 = 0$$
  
 $\langle \mathbf{p}_r + \lambda \mathbf{t}_r - \mathbf{c}, \mathbf{p}_r + \lambda \mathbf{t}_r - \mathbf{c} \rangle - r^2 = 0$ 

### Derivation

### Solving the equation:

$$\langle \mathbf{x}(\lambda) - \mathbf{c}, \mathbf{x}(\lambda) - \mathbf{c} \rangle - r^2 = 0$$
  

$$(\mathbf{x}(\lambda) - \mathbf{c})^2 - r^2 = 0$$
  

$$(\mathbf{p}_r + \lambda \mathbf{t}_r - \mathbf{c})^2 - r^2 = 0$$
  

$$(\lambda \mathbf{t}_r + (\mathbf{p}_r - \mathbf{c}))^2 - r^2 = 0$$

### **Result:** 1D Quadratic equation in $\lambda$ $\lambda^2 \mathbf{t}_r^2 + \lambda 2(\mathbf{t}_r \cdot (\mathbf{p}_r - \mathbf{c})) + (\mathbf{p}_r - \mathbf{c})^2 - r^2 = 0$

### Ray-Sphere Intersection (unit sphere)

For the unit sphere: center at origin, radius=1

$$\lambda^2 \mathbf{t}_r^2 + \lambda 2(\mathbf{t}_r \cdot \mathbf{p}_r) + \mathbf{p}_r^2 - 1 = 0$$

Spatial Data Structures Range Queries

### **Spatial Data Structures**

### **Range Queries**

#### Common problems

- Raytracing
- Select object by mouse click
- Collision detection

#### This should work on large models

- Scale to billions of primitives
- Asymptotic complexity

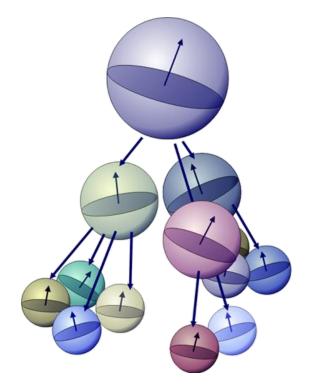
## **Spatial Data Structures**

### **Basic Idea:** Hierarchical decomposition

- If number objects too large:
  - Form spatially coherent groups
  - For each group:
    - Simple bounding volume
    - Apply recursively

### Result

- We obtain a tree of bounding volumes
- "Bounding volume hierarchy"



## **Bounding Volumes**

### **Axis-Aligned Bounding Box**

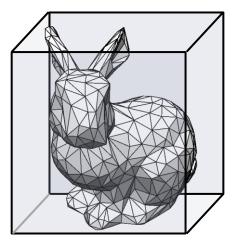
Store minimum x,y,z-coord

and

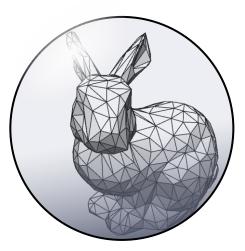
maximum x,y,z-coord

### **Bounding Sphere**

- Store radius, center
- Such that all geometry is contained



axis-aligned bounding box



bounding sphere

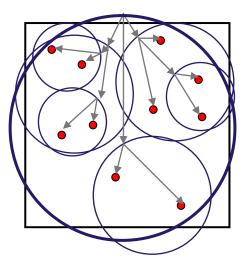
## Variants

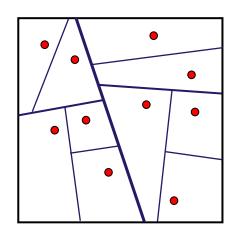
### Variants:

- Bounding volume hierarchy
  - General definition
  - Any bounding volumes
  - Image: spheres

#### BSP-tree

- Split planes (half-spaces)
- "Binary space partition tree"
- Arbitrary planes





## Variants

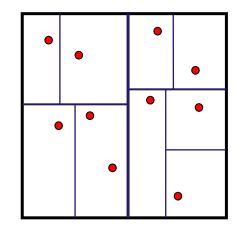
### Variants

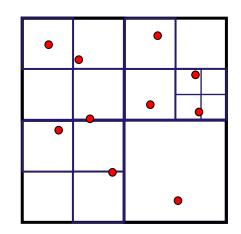
#### Axis aligned BSP tree / kD-tree

- Axis-parallel splitting planes
- Special case: kD-tree
  - Alternating splitting dimensions
  - Median cut: split at median coordinate

#### Quadtrees / Octrees

- Divide into 4/8 cubes
- Special case of the above (no binary tree though)





## **Extended Objects**

### **Extended objects (other than points)**

- Extended objects:
  - Triangles
  - Polygons
  - etc...
- Division of space might intersect with object
- Three solutions
  - Split objects (expensive, uncommon)
  - Overlapping nodes (common)
  - Storage multiple times (also common)

# Splitting Objects

#### First solution: *splitting*

#### • Example: Triangles in BSP tree

- Split at plane
- Aim at few splits

#### • (Rather) easy to see:

- General BSP tree needs still  $O(n^2)$  fragments (worst case, *n* triangles; practice:  $\approx O(n \log n)$ )
- Lower bound for kD trees, octrees, etc...

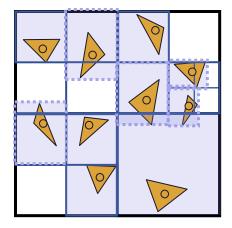
#### Splitting usually too expensive

Used in early low-polygon 3D engines (BSP-visibility)

# **Overlapping Regions**

### Second Solution: *overlap*

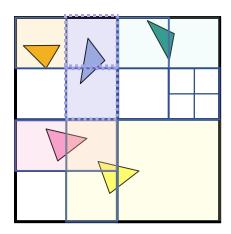
- Permit overlapping bounding volumes
- E.g., second bounding box (octree)
- Possible strategy:
  - Up to 10% oversize (in each direction)
  - No fit into leaf nodes: use an inner node
- Overlap reduces efficiency
  - Multi-coverage of volume
  - 10% in each direction means  $1.2^3 \approx 1.7 \times$
  - Effect on algorithms might vary



# **Overlapping Regions**

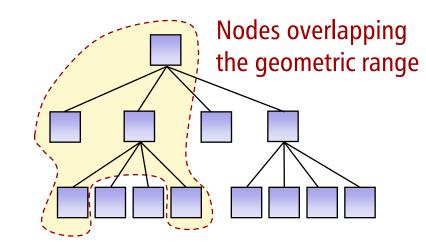
### Third Solution: *store multiple times*

- Store primitive multiple times
- Disadvantages
  - Reduced efficiency
  - Additional memory
- Advantages
  - Regular structures
  - No additional bounding boxes
- Common for raytracing



# **Range Queries**

## Range Query Algorithm

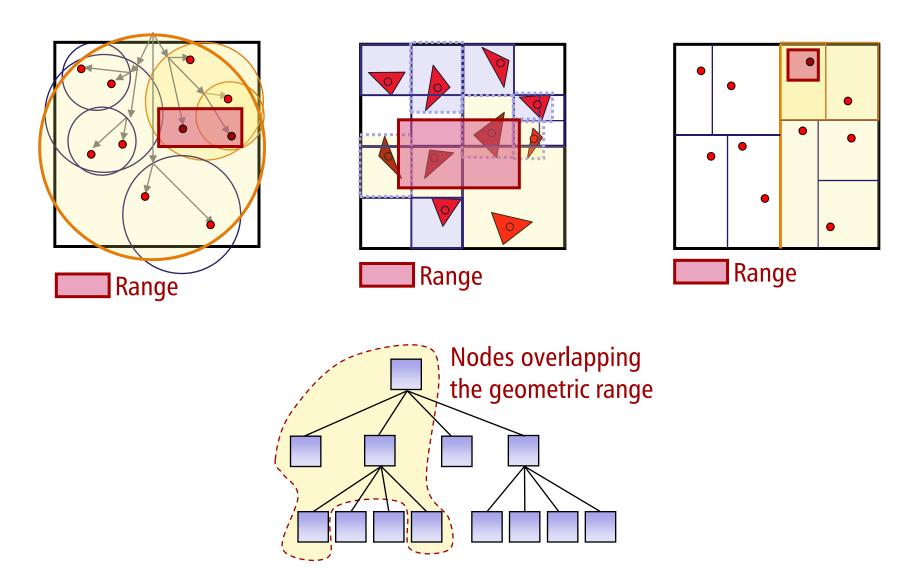


#### Start at root node: Then, recursively

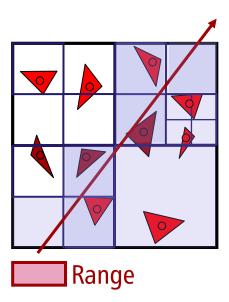
- If range overlaps bounding box
  - Test node primitives
    - Report if within range
  - Call recursively for child nodes
- If *range* does not overlap *bounding box*
  - End recursion

algorithm works for all hierarchy types

### Examples



## Raytracing



### Raytracing: special case

- Ray is the range
- Early ray termination
  - Sorted recursion (child closer to the camera: first)
  - Stop after hit

## In Practice

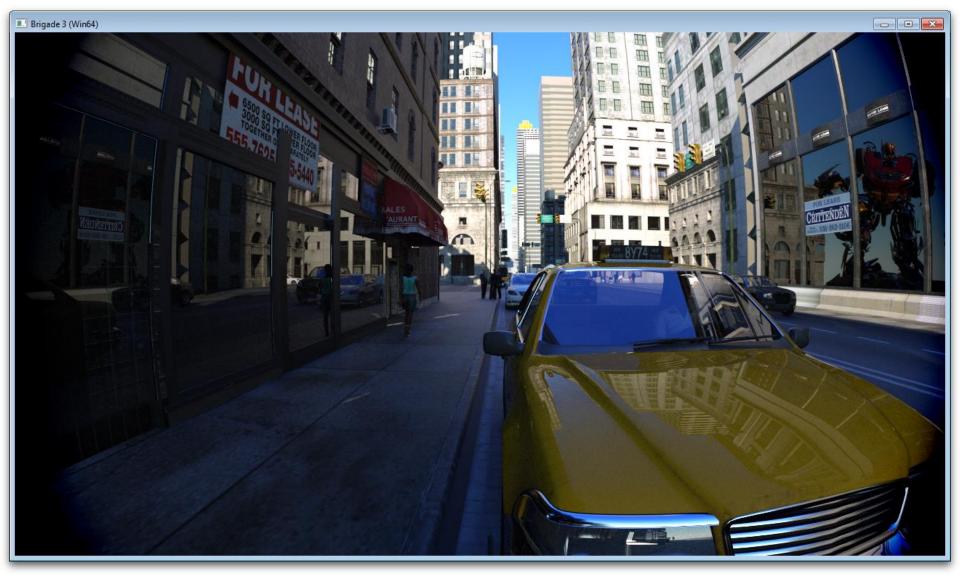
### **Significant Speedup**

- Simple implementation
  - Axis-aligned BSP tree
  - Single-core C++
  - 1.000.000 triangle scene
  - $\sim$  500.000 triangle-ray intersections per second

#### If you work harder...

- Optimized software  $\sim$ 15M
- GPU implementations up to 100M
- Optimized versions:
  - Performance also depends on ray coherence

### Brigade Renderer



**0.5-1 sec/frame on 2 × GeFoce GTX Titan** – http://raytracey.blogspot.nl/

### Brigade Renderer



realtime (youtube compression artifacts!) – Samuel Lapere / Youtube