

Introduction to Visualization and Computer Graphics DH2320, Fall 2015 Prof. Dr. Tino Weinkauf

#### Introduction to Visualization and Computer Graphics

Visibility Shading



# Visibility Algorithms



# **Two Rendering Pipelines**

### Rasterization

- Project all triangles to the screen
- Rasterize them (convert to pixels)
- Determine visibility
- Apply shading (compute color)

### Raytracing

- Iterate over all pixels
- Determine visible triangle
- Compute shading, color pixel
- next lecture

# Triangle / Polygon Rasterization



After Perspective Projection



## Rasterization

### Two main algorithms

- Painter's algorithm (old)
  - Simple version
  - Correct version

#### z-Buffer algorithm

Dominant real-time method today

# Painter's Algorithm

# Painter's Algorithm

### **Painters Algorithm**

- Sort primitives back-to-front
- Draw with overwrite

### Drawbacks

- Slowish
  - $\mathcal{O}(n \cdot \log n)$  for *n* primitives
  - "Millions per second"
- Wrong
  - Not guaranteed to always work







## **Counter Example**





### **Correct Algorithm**

- Need to cut primitives
- Several strategies
  - Notable: BSP Algorithm in Quake
  - Old graphics textbooks list many variants
  - No need for us to go deeper

# z-Buffer Algorithm

# z-Buffer Algorithm

### Algorithm

- Store depth value for each pixel
- Initialize to MAX\_FLOAT
- Rasterize all primitives
  - Compute fragment depth & color
  - Do not overwrite if fragment is farer away than the one stored the one in the buffer





color



depth



# Discussion: z-Buffer

#### Advantages

- Extremely simple
- Versatile only primitive rasterization required
- Very fast
  - GeForce 2 Ultra: 2GPixel /sec (release year: 2000)
  - GeForce 700 GTX Titan: 35 GPixel / sec (release year: 2013)

# Discussion: z-Buffer

#### Disadvantages

- Extra memory required
  - This was a serious in obstacle back then...
  - Invented 39 years ago (1974; Catmull / Straßer)

#### Only pixel resolution

Need painter's algorithm for certain vector graphics computations

#### No transparency

- This is a real problem for 3D games / interactive media
- Often fall-back to sorting
- Solution: A-Buffer, but no hardware support

# **Rasterization and Clipping**

## Rasterization

### How to rasterize Primitives?

### **Two problems**

- Rasterization
- Clipping











color

depth

## Rasterization

#### Assumption

- Triangles only
- Triangle not outside screen
- No clipping required

# **Triangle Rasterization**



Several Algorithms...

# **Triangle Rasterization**



**Example:** two slabs

# **Triangle Rasterization**



**Incremental rasterization** 

# **Incremental Rasterization**

### Precompute steps in x, y-direction

- For boundary lines
- For linear interpolation within triangle
  - Colors
  - Texture coordinates (more later)
- Inner loop
  - Only one addition ("DDA" algorithm)
  - Floating point value
  - Strategies
    - Fixed-point arithmetics
    - Bresenham / midpoint algorithm (requires if; problematic on modern CPUs)

## Rasterization

### How to rasterize Primitives?

### **Two problems**

Rasterization





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depth



#### **Crashes – write to off-screen memory!**

# **Clipping Strategies**

### **Pixel Rejection**

- "if (x,y ∉ screen) continue;"
  - Can be arbitrarily slow (large triangles)
  - Nope. Not a good idea.

### Screen space clipping

- Modify rasterizer to jump to visible pixels
  - See tutorial 5
- Efficient
- Still problems with when crossing camera plane
  (w = 0) ⇒ a semi-good idea



### Does not crash, optimal complexity

• O(k) for k output fragments

# Problem



#### **Problem:**

- Triangles crossing camera plane!
  - Wrong results
- Need object space clipping

## **View Frustum Clipping**









# **Further Optimization**

### **View Frustum Culling**

- Complex shapes (whole bunnies)
- Coarse bounding volume (superset)
  - Cube, Sphere
  - Often: Axis-aligned bounding box
- Reject all triangles inside if bounding volume outside view frustrum



Smooth Shading

Simple Shadows

**Global Illumination** 

# Shading Models



### **Reflectance Models**



# Interaction with Surfaces



#### **Local Shading Model**

- Single point light source
- Shading model / material model
  - Input: light vector l = (pos<sub>light</sub> pos<sub>object</sub>)
  - Input: view vector  $\mathbf{v} = (\mathbf{pos}_{camera} \mathbf{pos}_{object})$
  - Input: surface normal n (orthogonal to surface)
  - Output: *color* (RGB)

## Interaction with Surfaces



#### **General scenario**

- Multiple light sources?
  - Light is linear
  - Multiple light sources: add up contributions
  - Double light strength  $\Rightarrow$  double light output
# Remark

#### Simplify notation

Define component-wise vector product

$$\mathbf{x} \circ \mathbf{y} = \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} \circ \begin{pmatrix} y_1 \\ y_2 \\ y_3 \end{pmatrix} \coloneqq \begin{pmatrix} x_1 \cdot y_1 \\ x_2 \cdot y_2 \\ x_3 \cdot y_3 \end{pmatrix}$$

- No fixed convention in literature
- The symbol "o" only used in these lecture slides!

# Remark

#### **Lighting Calculations**

- Need to perform calculations for r, g, b-channels
- Often:

 $output_{r} = light_{r} \cdot material_{r} \cdot function(\mathbf{v}, \mathbf{l}, \mathbf{n})$   $output_{g} = light_{g} \cdot material_{g} \cdot function(\mathbf{v}, \mathbf{l}, \mathbf{n})$  $output_{b} = light_{b} \cdot material_{b} \cdot function(\mathbf{v}, \mathbf{l}, \mathbf{n})$ 

Shorter

# output = light\_strength • material · function(v, l, n)

# Shading Effects

#### Shading effects

- Diffuse reflection
- "Ambient reflection"
- Perfect mirrors
- Glossy reflection
  - Phong / Blinn-Phong
  - (Cook Torrance)
- Transparency & refraction

# Shading Effects

#### **Shading effects**

- Diffuse reflection
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# Diffuse ("Lambertian") Surfaces



surface color

## Diffuse ("Lambertian") Surfaces



## **Diffuse Reflection**



#### **Diffuse Reflection**

- Very rough surface microstructure
- Incoming light is scattered in all directions uniformly
- "Diffuse" surface (material)
- "Lambertian" surface (material)

# Surface Normal?

#### What is a surface normal?

- Tangent space:
  - Plane approximation at a point  $\mathbf{x} \in S$
- Normal vector:
  - Perpendicular to that plane
- Oriented surfaces:
  - Pointing outwards (by convention)
  - Orientation defined only for closed solids



# Single Triangle

Parametric equation

 $\{\mathbf{p}_1 + \lambda(\mathbf{p}_2 - \mathbf{p}_1) + \mu(\mathbf{p}_3 - \mathbf{p}_1) | \lambda, \mu \in \mathbb{R}\}\$ 

 $\mathbf{p}_1$ 

Triangles

**p**<sub>3</sub>

n

**p**<sub>2</sub>

- Tangent space: the plane itself
- Normal vector

$$(\mathbf{p}_2 - \mathbf{p}_1) \times (\mathbf{p}_3 - \mathbf{p}_1)$$

- Orientation convention:
  - **p**<sub>1</sub>, **p**<sub>2</sub>, **p**<sub>3</sub> oriented counter-clockwise
- Length: Any positive multiple works (often  $||\mathbf{n}|| = 1$ )



#### **Smooth Triangle Meshes**

- Store three different "vertex normals"
  - E.g., from original surface (if known)
- Heuristic:

Average neighboring triangle normals

## Lambertian Surfaces



normal vector (assuming:  $||\mathbf{n}|| = ||\mathbf{l}|| = 1$ )

## Lambertian Bunny



#### Face Normals



Interpolated Normals

# Shading Effects

#### Shading effects

- Diffuse reflection
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# "Ambient Reflection"

#### Problem

- Shadows are pure black
- Realistically, they should be gray
  - Some light should bounce around...
- Solution: Add constant



#### Not very realistic

 Need global light transport simulation for realistic results

# **Ambient Bunny**



#### **Pure Lambertian**



#### Mixed with Ambient Light

# Shading Effects

#### Shading effects

- Diffuse reflection
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# **Perfect Reflection**



#### **Perfect Reflection**

- Rays are perfectly reflected on surface
- Reflection about surface normal

 $\mathbf{r} = 2\langle \mathbf{n}, \mathbf{l} \rangle \mathbf{n} - \mathbf{l}$ 



# Silver Bunny

#### **Perfect Reflection**

- Difficult to compute
  - Need to match camera and light emitter
- More later:
  - Recursive raytracing
  - Right image: Environment mapping



Reflective Bunny (Interpolated Normals)

# Shading Effects

#### Shading effects

- Diffuse reflection
- "Ambient reflection"
- Perfect mirrors
- Glossy reflection
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- Transparency & refraction



#### **Glossy Reflection**

- Imperfect mirror
- Semi-rough surface
- Various models

# **Phong Illumination Model**

#### Traditional Model: Phong Model

- Physically incorrect (e.g.: energy conservation not guaranteed)
- But "looks ok"
  - Always looks like plastic
  - On the other hand, our world is full of plastic...

# How does it work?

#### **Phong Model:**



• Ambient part:

 $\mathbf{c} = \mathbf{c}_r \circ \mathbf{c}_a$ 

Diffuse part:

 $\mathbf{c} = \mathbf{c}_r \circ \mathbf{c}_l \cdot \langle \mathbf{n}, \mathbf{l} \rangle$ 

Add all terms together





# Blinn-Phong

#### **Blinn-Phong Model:**





Half-angle direction

$$\mathbf{h} = \frac{1}{2} \left( \frac{\mathbf{l}}{\|\mathbf{l}\|} + \frac{\mathbf{v}}{\|\mathbf{v}\|} \right)$$

- In the plane:  $\angle \left(\frac{\mathbf{h}}{\|\mathbf{h}\|}, \frac{\mathbf{n}}{\|\mathbf{n}\|}\right) = \frac{1}{2} \angle \left(\frac{\mathbf{r}}{\|\mathbf{r}\|}, \frac{\mathbf{v}}{\|\mathbf{v}\|}\right)$ 
  - Approximation in 3D

# Phong + Diffuse + Ambient Bunny



Blinn-Phong Bunny



#### **Interpolated Normals**

# Phong + Diffuse + Ambient Bunny



#### Blinn-Phong Bunny



#### **Interpolated Normals**

## **Better Models**





#### Phong Bunny

Cook-Torrance Model

# Shading Effects

#### Shading effects

- Diffuse reflection
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- Transparency & refraction

# Transparency

#### Transparency

- "Alpha-blending"
- *α* = "opacity"
- Color + opacity: RGBα

### Blending

• Mix in  $\alpha$  of front color, keep  $1 - \alpha$  of back color

$$\mathbf{c} = \alpha \cdot \mathbf{c}_{front} + (1 - \alpha) \cdot \mathbf{c}_{back}$$

- Not commutative! (order matters)
  - unless monochrome



# Refraction: Snell's Law

#### Refraction

- Materials of different "index of refraction"
- Light rays change direction at interfaces

## Snell's Law

$$\frac{\sin \theta_1}{\sin \theta_2} = \frac{n_2}{n_1}$$

- n<sub>1</sub>, n<sub>2</sub>: indices of refraction
  - vacuum: 1.0, air: 1.000293
  - water: 1.33, glass: 1.45-1.6



# Refraction



#### Implementation

- Not a local shading model
- Global algorithms: mostly raytracing
- Various "fake" approximations for local shading



#### Geometric Model



Color



# **Shading Algorithms**



# Flat Shading



Flat Shading constant color per triangle

# Flat Shading



"Gouraud Shading" Algorithm compute color at vertices, interpolate color for pixels

# Flat Shading



"Phong Shading" Algorithm interpolate normals for each pixel



#### **Geometric Model**



Color

# **Global Illumination:** next lecture



#### **Global Illumination**