## Circuit Analyses. Laboration 4 Measurements and simulations on AC-circuits.

This booklet, signed by the teacher, serves as a receipt for passing the lab. Each student must have a booklet of his own with solid preparation and completed readings.

Name:
Confirmed (Teacher):
Objective in this lab, you will learn how to implement ac voltage measurements of phase, amplitude and impedance. You should also use PSpice for AC-analyses.

## Equipment

- Oscilloskope DSO2014A
- Funktionsgenerator PM 5139 or the internal Wave-generator of the oscilloscope.
- Digital multimeter (DMM) Fluke45
- RCL-meter PM6303
- Breadboard and components

Litterature Presentations on the course web.
Report Write down your measured values, and figures, in this booklet and report to the teacher during the laboration.

## Preparation tasks, quick summary

## F1: Parameters of an AC-voltage

Assume that a sinusoidal ac voltage is mathematically described by the following relationship:

$$
u(t)=3 \sin (6280 t)
$$

Enter the peak-peak value ( $U_{\mathrm{t}-\mathrm{t}}$ ) RMS-value ( $U$ ) mean-value ( $\bar{U}$ ) frequency ( $f$ ), in the table.

## F2: Set up expressions for absolute value and phase for the RC-circuit.

 Set up an j $\omega$ expression for the transfer function of the RC link in the figure. Also, set up expressions for the absolute value and the the phase function.Calculate $U_{2}$ if the input volyage is the signal specified in F1 and $R=10$
 $\mathrm{k} \Omega$ and $C=10 \mathrm{nF} . \quad u(t)=3 \sin (6280 t)$

## F3: cutoff frequency

- How is the cutoff frequency defined?
- What is the absolute value and the phase value of the transfer function at the cutoff frequency?
- Calculate the cutoff frequency of the RC link in the figure (with $R=10 \mathrm{k} \Omega$ and $C=10 \mathrm{nF}$ ). $f_{\mathrm{g}}=$ ?


## F4: Prepare the Lin-Log-graph

In this booklet is a sheet with two charts. Both should have a linear $y$-scale ( $0 . .1$ for the absolute value and $0^{\circ} \ldots-90^{\circ}$ for phase). The frequency scale should be logarithmic and have the appropriate numbering. Also, provide values for the tick marks within the decades. Give the axles appropriate headings.

F5: Measuring impedance $L+r$ with the oscilloscope

$$
Z=\frac{U}{I} \quad Z=\sqrt{r^{2}+(2 \pi f \cdot L)^{2}} \quad \varphi=\arctan \frac{2 \pi f \cdot L}{r}
$$



During the lab you will measure an unknown coil with a series resistance. Derive an expression that can be for calculating $L$ and $r$ given $Z$ and $f$.
Calculations are simplified if you let the measurements take place at the phase angle $|\varphi|=45^{\circ}$.

$$
L=f(\mathrm{Z}, f) \quad r=f(\mathrm{Z}) \quad \text { at }|\varphi|=45^{\circ}
$$

F6: Measuring an impedance $L+C+r$ at resonance. The $\mathbf{Q}$-value.
Check what the Q value of a resonance circuit is about, and how it is calculated. How could the Q -value be calculated from the measured oscilloscope voltages?

## F7: Measuring impedance $L$ with the DMM

Higher accuracy in the measurement of $L$ can be obtained with the DMM. Derive an expression of how $L$ can be calculated if one measures the impedance of $Z_{1}$ and $Z_{2}$ at two different frequencies $f_{1}$ and $f_{2}$. $L=f\left(Z_{1}, Z_{2}, f_{1}, f_{2}\right)$

## Measurements, report of preparation tasks

F1, M1 Parameters of an AC-voltage
Assume that a sinusoidal ac voltage is mathematically described by the following relationship:

$$
u(t)=3 \sin (6280 t)
$$

Enter the peak-peak value ( $U_{\mathrm{t}-\mathrm{t}}$ ) RMS-value $(U)$ mean-value $(\bar{U})$ frequency ( $f$ ), in the table.

|  | peak-peak $\left(U_{\mathrm{t}-\mathrm{t}}\right)$ | RMS-value $(U)$ | meanvalue $(\bar{U})$ | frequency $(f)$ |
| :--- | :--- | :--- | :--- | :--- |
| Preparation |  |  |  |  |
| Measurement |  |  |  |  |

Set the function generator (or the oscilloscope's built-in-Wave Generator) so that the voltage is according to the preparatory task F1. Measure the voltage peak-peak value $\left(U_{t-t}\right)$ mean $(\bar{U})$, rms $(U)$, frequency $(f)$ with the oscilloscope. Fill in the answers in the table and check with preparation values from F1.

F2, F3, M2, M3: Set up expressions for absolute value and phase for the RC-circuit.

$\frac{\underline{U_{2}}}{\underline{U}_{1}}=$
$\left|\frac{\underline{\underline{U_{2}}}}{\underline{\underline{U}_{1}}}\right|=$

$$
\arg \left(\frac{\underline{U}_{2}}{\underline{U}_{1}}\right)=
$$

If $u(t)=3 \sin (2000 \pi t) \quad U_{2}=$ ?

## F3: Cutoff frequency

- How is the cutoff frequency defined? What is the absolute value and the phase value of the transfer function at the cutoff frequency?
- Calculate the cutoff frequency of the RC link in the figure (with $R=10 \mathrm{k} \Omega$ and $C=10 \mathrm{nF}$ ). $f_{\mathrm{g}}=$ ?
- Is the RC-link an HP LP BP or BS filter? Motivate your answer.

M2: Measuring absolute value and phase at one frequency
Connect the RC-circuit on the breadboard with $R=10 \mathrm{k} \Omega$ and $C=10 \mathrm{nF}$. Use input voltage $u(t)=3 \sin (2000 \pi t)$ as in M1. Connect the RC-link input and output to a respective channel of the oscilloscope.

It's the setting Phase $(2 \rightarrow 1)$ that gives you the correct sign for the phase.



|  | $\left\|\frac{\mid \underline{U_{2}}}{\underline{\underline{U}_{1}}}\right\|$ | $\arg \left(\frac{\underline{U_{2}}}{\underline{U}_{1}}\right)$ |
| :--- | :--- | :--- |
| Preparation |  |  |
| Measurement |  |  |

Does your measured values complies with your calculated values? If not, what can be the reason?

## M3: Measuring absolute value and phase as a function of frequency

Use same connections as in M2. Varying only the frequency of $U_{1}$. Measure the transfer function, absolute value an phase for frequencies $10 \mathrm{~Hz} . . .100 \mathrm{kHz}$ with "logaritmic steps" between points (1 $25 \ldots$ will bee enough cover). Tip! Set $U_{1}$ to $1,00 \mathrm{~V}$ on the oscilloscope - then $U_{2}$ will directly display the attenuation without any calculations!)

## Frekvensgång, Gränsfrekvens

| frekvens | 10 Hz | 20 Hz | 50 hz | 100 Hz | 200 Hz | 500 Hz | 1 kHz | 2 kHz |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\left\|\frac{\underline{U_{2}}}{\underline{\underline{U}_{1}}}\right\|$ |  |  |  |  |  |  |  |  |
| $\arg \left(\frac{\underline{U}_{2}}{\underline{U}_{1}}\right)$ |  |  |  |  |  |  |  |  |
| frekvens | 5 khz | 10 kHz | 20 kHz | 50 kHz | 100 kHz | $f_{\mathrm{g}}$ |  |  |
| $\left\|\frac{\underline{U}_{2}}{\underline{U}_{1}}\right\|$ |  |  |  |  |  |  |  |  |
| $\arg \left(\frac{\underline{U}_{2}}{\underline{U}_{1}}\right)$ |  |  |  |  |  |  |  |  |

Then vary the frequency free to determine the cutoff frequency as closely as you can. The cutoff frequency is best determined by phase measurement.

M3, F4: Plot the results of your measurements in the chart that you have prepared.



## M4: Simulation of a time sweep (time domain, transient)

Perform a time sweep corresponding to the measurement of M2, ie shows input and output voltage as a function of time (as on the oscilloscopescreen). Draw the curves in Probe and print the result / show the labassistant.

## M5: Simulation of a frequency sweep (AC Sweep)

Perform an AC analysis, AC Sweep, which corresponds to the measurement of M3, which gives the am attenuation and phase angle as a function of frequency. Draw curves in Probe and print the result / show the labassistant.
(If you wish, you can alternatively express the amplitude in decibel DB. Curves then form a socalled Bode diagram.)


At the lab you will measure an unknown coil with a series resistance. Oscilloscopes can only measure voltages. A measuring resistor $R=10 \Omega$ will have a voltagedrop proportional to the current. Another limitation is that both oscilloscope channels and the signal generators share the same common ground. This forces us to use external voltmeter connection.
As the signal generator you can use the PM5139 or oscilloscope's in-built-Wave generator.
Swipe the frequency starting with 50 Hz to about 5 kHz and write down the approximate frequencies when the phase angle is $30^{\circ}, 45^{\circ}, 60^{\circ}$. Measure the frequency of $45^{\circ}$ carefully.

Measurement of frequency for three phase angles

| $\varphi=30^{\circ} \approx f_{30}[\mathrm{~Hz}]$ | $\varphi=45^{\circ} f_{45}[\mathrm{~Hz}]$ | $\varphi=60^{\circ} \approx f_{60}[\mathrm{~Hz}]$ |
| :--- | :--- | :--- |
|  |  |  |

Preparation task F5, write down your expressions for $L$ and $r$ at $45^{\circ}$ :
$r\left(\varphi=45^{\circ}\right)=f\left(Z_{45}\right)=\quad L\left(\varphi=45^{\circ}\right)=f\left(Z_{45}, f_{45}\right)=$
Measurment with oscilloscope at $45^{\circ}$ calculated values. Note! You can "draw" the value of the known measuring resistor $R 10 \Omega$ from your calculated value of $r$ !

| $L=[\mathrm{mH}]$ | $r=[\Omega]$ |
| :--- | :--- |
|  |  |

## M7: Serieal resonance circuit $L+C+r$ with oscilloscope



Add a series capacitor $\mathrm{C}=330 \mathrm{nF}$, so that impedance now is a series resonant circuit. Search for the resonance frequency $f_{0}$. It is characterized in that the current $I$ has it's maximum (Ch1 max).

- Vilken Which phase angle $\varphi$ between current and voltage has the impedance then?
$f_{0}($ measured $)=\quad[\mathrm{Hz}]$
Calculate the resonance frequency with the value of $L$ from M6: $\quad f_{0}=\frac{1}{2 \pi \sqrt{L \cdot C}}=$


## F6, M8: Measuring an impedance $L+C+r$ at resonance. The $\mathbf{Q}$-value.



At the resonance frequency. Switch the oscilloscope's Channel 1 so that you measure the voltage across the capacitor. (Now $R$ can be shorted because we no longer need to measure the current.)

- What is the voltage over $C$ ? $\quad U_{\mathrm{Ch} 1}=\quad[\mathrm{V}]$

What is the feeding voltage on the circuit? $U_{\mathrm{Ch} 2}=\quad[\mathrm{V}]$

- How do you explain this "mystery" ?

F6 How can the Q-value be calculated directly from the measured values?)

- The inductor's Q -value at our resonance frequency. $\quad Q=$


## F7, M9: Measuring impedance $L$ with the DMM



A more accurate measurement of the coil impedance can be done with DMM. It has no common ground with the signal generator (or oscilloscope wave generator) so you can then select "inner voltmeter connection". Connect the inductor on the breadboard for measuring current and voltage with the DMM. Measure the impedance at two frequencies, the frequency when $\varphi$ according to $\mathbf{M 6}$ vas $30^{\circ}$, and the frequency when $\varphi$ was about $60^{\circ}$ (we take measurements of both sides of the impedance cutoff frequency). Measure frequency thoroughly with DMM.

F7. Your expression for calculation of $L$ based on the two measurements:

$$
L=f\left(Z_{60}, Z_{30}, f_{60}, f_{30}\right)=
$$

Fill in your measured values

| Beräkna $Z=\frac{U}{I}$ |  | $f[\mathrm{~Hz}]$ |  |
| :---: | :---: | :---: | :---: |
| $Z_{30}\left(\varphi \approx 30^{\circ}\right)$ | $Z_{60}\left(\varphi \approx 60^{\circ}\right)$ | $f_{30}\left(\varphi \approx 30^{\circ}\right)$ | $f_{60}\left(\varphi \approx 60^{\circ}\right)$ |
|  |  |  |  |

Calculated impedance

$$
L=\quad[\mathrm{mH}]
$$

## M10: Checking with the RCL-meter

| $L=[\mathrm{mH}]$ | $r=[\Omega]$ |
| :--- | :--- |
|  |  |

- How good was the oscilloscopemesurement?
- How good was the DMM-measurement?

Your comments:

