IE1206 Embedded Electronics



Quick Formula for exponential





• More complex circuits one simplifies with equivalent circuits to one of these elementary shapes. (If this is not possible advanced courses will have a transform methood available).

Continuity requirements Summary $\stackrel{c}{\vdash}$ The Capacitor has voltage inertia

In a capacitor, charging is always continuous The capacitor **voltage is always continuous**.

The Inductor has current inertia

In an inductor the magnetic flux is always continuous In an inductor **current is always continuous**.

"All" by "the rest"



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Draw function $u_{\rm C}(t)$



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 $u_{\rm C\infty} = 15 \text{ V}$
 $\tau = 2000 \cdot 1000 \cdot 10^{-6} = 2 \text{ s}$



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.

t =0 R $R = 2000 \Omega$ and $C = 1000 \mu F$ 15 V Obtain an expression for $u_{\rm C}(t)$ + +5 V U_{\cap} Draw function $u_{\rm C}(t)$ Calculate how long it takes for $u_{\rm C}$ to reach +10V? $x(t) = x_{\infty} - (x_{\infty} - x_0) \cdot e^{-\frac{1}{\tau}}$ $u_{\rm C0} = 5 \, {\rm V}$ $u_{\rm C\infty} = 15 {\rm V}$ $u_{c}(t) = 15 - (15 - 5) \cdot e^{-\frac{t}{2}} = 15 - 10 \cdot e^{-0.5 \cdot t}$ $\tau = 2000 \cdot 1000 \cdot 10^{-6} = 2 \text{ s}$

Note: Capacitor voltage is continuous – If you put a voltage across a capacitor it can not charge instantaneously (would require infinite current). The voltage will not change at once.

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Neon lamp (10.9) DANGER OLTAGE R_1 600k Ω S On 65V Off 55V Ε 200V С + R_2 **400k**Ω u (t) 2,2 μF 0



Flash-circuit with neon lamp.

Neon lamp (10.9)



a) When will the first flashing light be?



The capacitor is charged from 0V up to 80V at 65V the neon lamp lights up (and discharges the capacitor to 55V when it goes off).

$$\tau = R_I \cdot C = 240 \cdot 10^3 \cdot 2, 2 \cdot 10^{-6} = 0,528$$
$$t = \tau \cdot \ln \frac{all}{rest} = 0,528 \cdot \ln \frac{80 - 0}{80 - 65} = 0,88 s$$

Neon lamp (10.9)



b) *How long will it take until the next blink?*

The capacitor is now charging from 55V up to 80V at 65V when the neon lamp lights up (and discharges the capacitor to 55V, then it goes off).



Neon lamp (10.9)



c) If R_2 is removed, how long does it then between flashes?



If R_2 is removed *E* will not be votage divded. E = 200. Timeconstant will be changed.

The capacitor is charging now from 55V up to 200V at 65V when the neon lamp lights up (and discharges the capacitor to 55V when it goes off).

$$\tau = R_1 \cdot C = 600 \cdot 10^3 \cdot 2, 2 \cdot 10^{-6} = 1,32$$
 Flash frequency:
$$t = \tau \cdot \ln \frac{all}{rest} = 1,32 \cdot \ln \frac{200 - 55}{200 - 65} = 0,094 \ s \qquad f = \frac{1}{T} = \frac{1}{0,094} = 11 \text{ Hz}$$

Schmitt-trigger (10.10)



Trigger levels? (10.10)



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RC-oscillator (10.10)



The comparator charges the capacitor to the upper trigger level, then it turns the output on and discharges the capacitor to the lower trigger level. The frequency of the output of the comparator depends on the product $R \cdot C$. Since *C* is constant so will the *R* controls the frequency.

RC-oscillator frequency (10.10)



$$\tau = R \cdot C = 5 \cdot 10^3 \cdot 150 \cdot 10^{-9} = 0,75 \cdot 10^{-3}$$

$$t_1 = \tau \cdot \ln \frac{all}{rest} = 0,75 \cdot 10^{-3} \cdot \ln \frac{5 - \frac{1}{3} \cdot 5}{\frac{1}{3} \cdot 5} = 0,75 \cdot 10^{-3} \cdot \ln 2 = 5,2 \text{ ms}$$

$$t_2 = t_1 \quad T = 2 \cdot t_1 = 2 \cdot 5, 2 \cdot 10^{-3} = 10,4 \text{ ms} \quad f = \frac{1}{T} = \frac{1}{10,4 \cdot 10^{-3}} = 962 \text{ Hz}$$

The supply voltage 5V went shorten away. The frequency is thus independent of changes in the supply voltage!

E is a DC source. At the time t_1 the switch is closed.



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a) How large is the current through the coil in the first moment?





Answer: The inductor has has "current inertia". The first moment (t_1) the current will be the "same" i = 0.

b) How large is the current through the inductor after a long time interval?



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Answer: After a long time, the changes have faded away. The voltage across the inductor (is due to changes) then is 0, the inductor is "shorting" the 100 Ω parallel resistor. The 100 Ω series resistor limits the current from the voltage source. $i = 10V/100\Omega = 0.1$ A.

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Inductor connection and **disconnection** (10.8) After switch opening Before switch opening $t_1 < t < t_2$ **100** Ω 0,1 A $t_{2} < t$ Without 0,1 A . i _L ⁺10 V current Ε +++**100** Ω **100** Ω 1 H 10 V 1 H =0V $u_{\rm R}$



After t_2 the current starts from the "same value" 0,1 A (i_0) as before the switch opening, and then the current will decrease down to 0 (i_{∞}). Time constant will be $\tau = L/R = 1/100 = 0,01$ s.



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Quick formula:
$$x(t) = x_{\infty} - (x_{\infty} - x_0)e^{-\frac{t}{\tau}}$$

 $i_{L_{\infty}} i_{L_{\infty}} i_{L_{0}} i_{L_{0}} = \frac{t}{0.01} \iff i_{L}(t) = 0, 1 \cdot e^{-\frac{t}{0.01}} = 0, 1 \cdot e^{-100 \cdot t}$



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Snabbformeln:
$$x(t) = x_{\infty} - (x_{\infty} - x_0)e^{-\frac{t}{\tau}}$$

 $i_{\rm L}(t) = 0 - (0 - 0, 1) \cdot e^{-\frac{t}{0,01}} \iff i_{\rm L}(t) = 0, 1 \cdot e^{-\frac{t}{0,01}} = 0, 1 \cdot e^{-100 \cdot t}$



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When the voltage source 10 V is disconnected, the current is driven by the inductor. The voltage drop over the 100 Ω resistor U_R at first is -100.0,1 = -10 V. The minus sign comes from the fact that the current is entering the resistor in the part of the resistor we defined negative.



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• Suppose the resistor is 1000 Ω . Then u_R at first moment had been -100 V !



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- Suppose the resistor is 1000 Ω . Then u_R at first moment had been -100 V !
- Suppose the resistor is 10000 Ω then the voltage had been -1000V !



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- Suppose the resistor is 10000 Ω then the voltage had been -1000V !

• When the circuit is broken the inductor tries to "keep" the current, until all the magnetic energy has been consumed. If you omit the resistor from the circuit, ie, $R = \infty$ there will be a very high voltage.

Ex. To break the current to a coil will produce a high voltage

