

Solutions:

1

(a)

Homog	Inhomog
Nd:YAG	Nd:glass fiber
Ti:Sapphire	Er:glass fiber
Yb:YAG	He-Ne
GaAs	Ar ⁺ ion plasma
Alexandrite	CO ₂
Ruby	

(b) Nd:YAG collisional phonon, Ti:Sapphire collisional phonon (vibronic), He-Cd Doppler, isotope, Nd:glass local field, collisional.

(c)

$$\tau_{sp} = \frac{3h\varepsilon_0 c^3}{16\pi^3 n \nu_0^3 |\mu|^2}$$

$$g(0) = \frac{2}{\pi \Delta \nu_0}$$

$$\sigma(0) = \frac{2\pi^2 |\mu|^2}{3n\varepsilon_0 c h} \nu_0 g(0)$$

$$\tau_{sp} = \frac{\lambda_0^2}{4\pi^2 n^2 \sigma(0) \Delta \nu_0} \cdot 1$$

2.

(a) Whole line in homogeneous medium, spectral hole burning in inhomogeneous medium.

(b) Partly-forbidden – longer lifetime.

(c) Calculate G_0 , Γ_s , then use

$$I(l) = \Gamma_s \ln \left(1 + \left(\exp \left(\frac{\Gamma_{in}}{\Gamma_s} \right) - 1 \right) G_0 \right)$$

3.

(a) all except KTiOPO₄. Inversion symmetry.

(b) no. No accumulation of energy.

(c) 1064/2. 1319/2. 1319/3

Task 4

- (a) Monochromaticity, Coherence, Directionality, Brightness
 (b) When a laser beam scattered from a rough surface, the scattered light is seen to consist of a random collection of alternately bright and dark spots.
 (c) $d_g = 2\lambda L/D$, so $L = 237$ cm.
 (d) 1.67 mm.

Task 5.

- (a) ...
 (b)

$$\omega' = \left[\omega^2 - \left(\frac{1}{t_0} \right)^2 \right]^{1/2}$$

$$t_0 = \frac{2\tau}{x}$$

$$\omega = \left[\frac{(x-1)}{\tau_c \tau} \right]^{1/2}$$

$$\tau_c = \frac{L_e}{\gamma c}$$

$\tau = 230$ μ s, $\tau_c = 34$ ns, $x = 2$, $\omega = 355$ KHz, $t_0 = 230$ μ s, so ω' is 355 KHz.

- (c) Homogenously broadened,

$$\Delta\tau_p \cong \frac{0.45}{(v_m \Delta\nu_0)^{1/2}}$$

$v_m = c/2L = 750$ MHz, $\Delta\tau_p = 37$ ps.

Inhomogenously broadened,

$$\Delta\tau_p \cong \frac{0.441}{\Delta\nu_0^*}$$

$\Delta\tau_p = 2.3$ ps.

- (d) $E = \int_{-\infty}^{+\infty} P(t) dt$

$P_{av} = v_m E$, so $P_p = 442.5$ W, $E = 5$ nJ.

Task 6

(a)
$$P_{th} = \left(\frac{\gamma}{\eta_p} \right) \left(\frac{h\nu_p}{\tau} \right) \left(\frac{\pi a^2}{\sigma_e \{1 - \exp[-(2a^2/w_0^2)]\}} \right), 54.25 \text{ W}$$

(b)
$$P_{th} = \left(\frac{\gamma}{\eta_p} \right) \left(\frac{h\nu_p}{\tau} \right) \left[\frac{\pi(w_0^2 + w_p^2)}{2\sigma_e} \right], 24.77 \text{ W (The pumping efficiency } \eta_p = \eta_a T_p = [1 - \exp(-\alpha l)] T_p)$$