

SK2411, IO2659 VT2009 Exam solutions

Task 1

(a)

$$\frac{P_{out}}{P_p} = A_b I_s \frac{\gamma_2}{2} \frac{1}{P_{th}}$$

$$P_{th} = \frac{\gamma h \nu_p \pi (w_o^2 + w_l^2)}{2 \eta_p \tau \sigma_e}$$

$$I_s = \frac{h\nu}{\sigma\tau}, A_b = \pi w_0^2, \gamma = \gamma_2/2,$$

$$\frac{P_{out}}{P_p} = \eta_p \frac{h\nu_e}{h\nu_p}$$

(b)

$$P_h = P_{out} \left(\frac{\lambda_e}{\lambda_p} - 1 \right)$$

Nd:YAG 31.7W

Yb:YAG 10.6 W

Task 2.

(a) ..

(b) ..

(c)

$$\frac{P_{ih}}{P_h} = \frac{\sigma_h \tau_h}{\sigma_{ih} \tau_{ih}} = \frac{\Delta v_{ih} \tau_h}{\Delta v_h \tau_{ih} \sqrt{\pi \ln 2}} = 207.8$$

Task 3.

(a) (i)

(b) Excimer

(c)

$$h\nu_{J'+1} - h\nu_{J'} = 2B$$

Task 4.

(a) ...

$$(b) \begin{bmatrix} 1 & 0 \\ \frac{n_1-n_2}{n_1 R_1} + \frac{n_2-n_1}{n_1 R_2} & 1 \end{bmatrix}, \text{ so } f = \frac{n_2-n_1}{n_1} \left(\frac{1}{R_2} - \frac{1}{R_1} \right)$$

(c) At far field, $\theta_d = \lambda/\pi w_0$, so $w_0 = 0.632 \times 10^{-3} \text{ mm}/(\pi \times 10^{-3} \text{ rad}) = 0.2 \text{ mm}$.

$$P = (\pi w_0^2 / 2) I_0, \text{ so } I_0 = 79.5 \text{ mW/mm}^2.$$

Task 5.

(a) ...

(b) Radiative efficiency, transfer efficiency, absorption efficiency, and quantum efficiency.

(c) The elemental power dP absorbed within volume dV can be written as $dP = [I_p(r,z) - I_p(r,z+dz)]dS = -dI_p/dz * dz dS = -\alpha I_p(r,z) dV$. By definition, we then have

$$dP = R_p h \nu_p dV, \text{ so } R_p(r,z) = -\alpha I_p(r,z) / h \nu_p.$$

Task 6.

(a) ...

$$(b) R_{cp} = (fNt + Nc)/(1+f)\tau$$

$$(c) \gamma = \gamma_1 + (\gamma_1 + \gamma_2)/2 = 0.03 + (-\ln R1 - \ln R2)/2 = 0.05. Nc = \gamma/\sigma_e l = 3.08 \times 10^{17} \text{ cm}^{-3}.$$

$$(d) \Delta\tau_p = \frac{0.441}{\Delta v_L} = \frac{0.441}{11 * 3E10} = 1.33 \text{ ps}.$$